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COMPOSITE LAMINATE WEIGHT OPTIMIZATION ON THE SHARP
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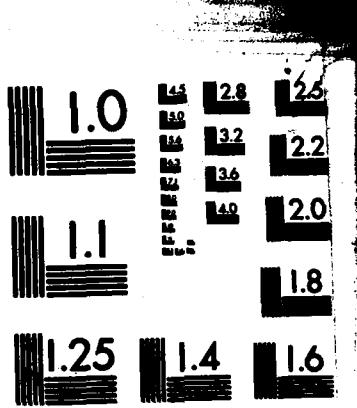
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**COMPOSITE LAMINATE WEIGHT OPTIMIZATION ON THE SHARP PC-1500
POCKET COMPUTER**

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August 1983

Final Report for Period June 1983 - October 1983

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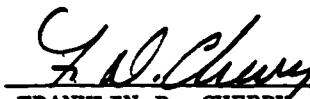
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Mechanics and Surface Interactions Branch
Nonmetallic Materials Division

FOR THE COMMANDER



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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) An automated composite laminate sizing technique is presented, which optimizes for minimum weight. The technique can be coded for a microcomputer and a listing is given for the Sharp PC-1500. The program is interactive and easy to use. Ply ratios are optimized for point stress under multiple independent loads.		

FOREWORD

This report was prepared in the Mechanics and Surface Interactions Branch (AFWAL/MLBM), Nonmetallic Materials Division, Materials Laboratory, Air Force Wright Aeronautical Laboratories, Wright-Patterson Air Force Base, Ohio. The work was performed under the support of Project Number 2307, "Nonmetallic Structural Materials", Task Number 2307P2, "Composite Materials and Mechanics Technology," and under Contract F33615-83-C-5001.

In this report, an automated composite laminate sizing technique is presented, which optimizes for minimum weight. The technique can be coded for a microcomputer and a listing is given for the Sharp PC-1500. The program is interactive and easy to use. Ply ratios are optimized for point stress under multiple independent loads.

This program is available on cassette tape and can be obtained by sending a blank 15 or 30-minute tape to AFWAL/MLBM, Wright-Patterson AFB, Ohio 45433 and referencing this report.

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SECTION I

PROGRAM DESCRIPTION

The program "OPTIM" is an optimization program designed to run on a small microcomputer. The listing presented here is for a Sharp PC-1500 with an 8K memory expansion. The version of Basic is standard enough that translations to other microcomputers is possible.

The program will find a minimum thickness laminate which will not fail under any of the load conditions entered. Ply orientations are chosen by the user. The program's capability in handling multiple, independent, loads could be useful for loads which change with time or for situations where there is uncertainty in calculating the loads. As the program is currently dimensioned, four independent load combinations and 6-ply orientations can be entered.

Only point stresses are considered, thus the program optimizes the laminate only at one point in the structure. Furthermore, the program assumes in-plane loads only and no out of plane deflections. This implies a symmetric laminate, but stacking sequence is not a factor in the program. The layer thicknesses generated by the program are the total and must be divided by 2 to get the halves of a symmetrical laminate.

No knowledge of optimization techniques is needed to run the program and very little knowledge of laminate plate theory is needed. In addition, material properties for three common advanced composites are stored in the program and new composite materials can be added by inputting their material constants into the program directly.

SECTION II

GENERAL INSTRUCTIONS

The Sharp PC-1500 manual includes tape loading instructions. Because "OPTIM" takes so long to read (approximately 5 minutes), it's a good idea to test tape player volume level with a short one or two line program to see if all is well. Load the tape using "OPTIM" as the name. An example of the display and appropriate responses are given in this report.

The program is started in RUN mode by instruction RUN (press the keys [R] [U] [N] and [ENTER]). User is guided through the program by simple questions. The user types the chosen answer and presses the [ENTER] key. At the completion of the routine, after all results have been displayed, the program will restart itself.

Run times can be quite long. They range from a minute for a 2-layer laminate, to 10 minutes for a 6-layer laminate subject to multiple loads.

The material constants are stored in the program. When "MATERIAL NO. = " is asked, input the material number;

1....T300/5208

2....BORON/5508

3....AS/3501

To add other materials (up to 6 more), user should type (in PRO mode) for a material with the material number N,

16NG: DATA "name of material", E_x , E_y , v_x , E_s , h_0 , X , X' , Y ,
 Y' , S : RETURN.

An example of adding a new material (Aluminum...Material number 4) is as follows:

Set PRO Mode and type,

1640 DATA "ALUMINUM", 69, 69, .3, 26.538, 125E-6, 400, 400, 400, 230 :

RETURN

and press ENTER key.

The unit of engineering constants are in GPa and thickness of single ply
 h_0 is in meters.

SECTION III

METHOD

The goal is to minimize the total thickness of a composite laminate subject to failure constraints under static loads. Specifically

$$\sum_{k=1}^L h_k = \text{min.} \quad \text{where } L = \text{number of layers}$$

subject to $h > 0$ and $G_{ij}^{(0,k)} \epsilon_i^{(N)} \epsilon_j^{(N)} + G_i^{(0,k)} \epsilon_i^{(N)} - 1 \leq 0$ where h_k is the total thickness of all the plies at the k 'th orientation (which will be referred to as a "layer" in this report). The failure criteria is a first ply failure based on the Tsai-Wu tensor criteria in strain space. The G 's are transformed to the laminate axis from the k 'th layers orientation. The strains are associated with the N 'th loading combination. This distinction is made since more than one independent loading may be considered. For the definition of the G 's in terms of experimental strength data, see reference 1.

Stacking sequence is not included in this formulation, and the laminate is assumed not to bend or warp. Therefore, strains and loads are related by

$$\vec{N} = |A| \vec{\epsilon}$$

The optimization method applied is a modification of the method of feasible directions. The method can be demonstrated graphically with 2-dimensions, i.e. two layers. In figure 1 the two equalities

$$G_{ij}^{(0)} \epsilon_i \epsilon_j + G_i^{(0)} \epsilon_i - 1 = 0$$

$$G_{ij}^{(90)} \epsilon_i \epsilon_j + G_i^{(90)} \epsilon_i - 1 = 0$$

have been plotted as functions of $h^{[0]}$ and $h^{[90]}$ for the single loading condition shown. Any point above and to the right of these two curves is feasible, that is, failure will not occur. Points to the left and below the curves are infeasible. Because our objective function (the sum of the layer thicknesses) is linear, the optimum point will lie on one of these curves or the intersection of multiple curves.

The program starts by finding an initial feasible point (A) which lies on a constraint curve farthest from the origin on the line $h^{[90]}=h^{[0]}$. The distance from the origin is calculated using a strain ratio method. Along any vector which passes through the origin

$$h_k^{i+1} = h_k^i \cdot S/S_0$$

where S is a scalar distance, and $S_0 = [\sum_{k=1}^L (h_k^i)^2]^{1/2}$

along this vector, strain can be found using

$$\epsilon_i^0 = \frac{\epsilon_i^0 S_0}{S}$$

where ϵ_i^0 is a component of laminate strain evaluated at S_0 .

Substituting into the failure criteria we have

$$\frac{G(\theta_k) \epsilon_i^0 S_0^2}{S^2} + \frac{G_i(\theta_k) \epsilon_i^0 S_0}{S} - 1 = 0$$

To ensure the calculated point lies slightly in the feasible region despite any numerical error, the program sets this function equal to the negative of a small number $1E(-6)$ rather than zero. Solving this equation for positive S we have

$$S = \frac{-B + \sqrt{(B^2 - 4AC)}}{2A}$$

where

$$A=1-1E-6 \quad B=\sum_{i=1}^3 -G^{(\theta_k)} \epsilon_i^o S_0$$

$$C=\sum_{i=1}^3 \sum_{j=1}^3 -G^{(\theta_k)} \epsilon_i^o \epsilon_j^o S_0^2$$

If S_0 lies in the feasible region we solve the above equation for each layer and each load combination then take the smallest resulting S as the one that defines the boundary of the feasible region.

The next step in the optimization procedure is to establish a direction vector which will point away from the constraint A lies on and is parallel to the plane defined by $\sum h_k = \text{constant}$. In figure 1, this direction is shown as Z . Finding Z first requires calculation of the gradient of the active constraint evaluated at A . Let

$$c_{k,N} = G_{ij}^{(\theta_k)} \epsilon_i^{(N)} \epsilon_j^{(N)} + G^{(\theta_k)} \epsilon_i^{(N)} - 1$$

where k and N correspond to the layer and load combination of the active constraint. A constraint is considered active if $c_{k,N} > -E_2$ where $E_2=1E-5$ is a small number. Note that more than one constraint may be active. The gradient is then given by

$$\vec{\nabla} c_{k,N} = \sum_{L=1}^L [G_{ij}^{(\theta_k)} \left(\frac{\partial \epsilon_i^{(N)}}{\partial h_L} \epsilon_j^{(N)} + \epsilon_i^{(N)} \frac{\partial \epsilon_j^{(N)}}{\partial h_L} \right) + G^{(\theta_k)} \frac{\partial \epsilon_i^{(N)}}{\partial h_L}] \hat{h}_L$$

where \hat{h}_L is a unit vector. To find the partials of strain we start with the basic equation

$$\vec{N} = |A| \vec{\epsilon}$$

$$0 = \frac{\partial}{\partial h_i} |A| \vec{\epsilon} + A \frac{\partial}{\partial h_i} \vec{\epsilon}, \frac{\partial \vec{\epsilon}}{\partial h_i} = -|A^{-1}| \frac{\partial}{\partial h_i} |A| \vec{\epsilon}$$

and

$$\frac{\partial}{\partial h_i} |A| = \begin{bmatrix} (\theta_i) & (\theta_i) & (\theta_i) \\ Q_{11} & Q_{12} & Q_{13} \\ \\ (\theta_i) & (\theta_i) & (\theta_i) \\ Q_{21} & Q_{22} & Q_{23} \\ \\ (\theta_i) & (\theta_i) & (\theta_i) \\ Q_{13} & Q_{23} & Q_{33} \end{bmatrix} = [Q_i]$$

The gradient vector is normalized to unit length. If more than one constraint is active, the normalized gradients are summed together and the sum is then normalized to one. The negative of the gradient will point away from the constraint, into the feasible region. This vector is now projected onto the plane defined by the unit normal \hat{n} , where

$$\hat{n} = \frac{1}{\sqrt{L}} \sum_{i=1}^L \hat{h}_i .$$

The projection can be made with a double cross product

$$\vec{z} = \hat{n} \times (-\bar{\nabla}c \times \hat{n}) .$$

With a vector identity, this can be rewritten as

$$\vec{z} = (\bar{\nabla}c \cdot \hat{n})\hat{n} - \bar{\nabla}c .$$

Finally, \vec{z} is also normalized to unit length.

Along \vec{z} , another constraint will eventually be reached (point B in Figure 1). The point is found iteratively by a bisection technique. Since the bisection method is very time consuming, the constraint line is only found within a relatively large error band. What we are really interested in is a point approximately midway between A and B, which is C in the figure. From point C, the strain ratio technique is used to analytically calculate D. Starting at D, the entire procedure repeats.

The program terminates when the distance \overline{AB} or \overline{CD} is small (say 1/10 of a
ply thickness) or the magnitude of \vec{Z} before normalization is very small
(implying \hat{n} and \vec{v}_c are almost parallel).

In some cases, $h_k \geq 0$ constraint may be reached. When this happens,
that orientation is completely dropped from further calculations. Thus,
the constraints associated with a zero thickness layer cannot affect the
results. Once an orientation reaches zero thickness, it is never
reinstated in later iterations.

Figure 1 shows a case where the program reaches the intersection of
two constraints. However, simultaneous failure should not be considered
a criteria for optimization. The constraint line for the +45° layer is
completely in the infeasible region. The line $h^{[45]} + h^{[-45]} = \text{const.}$
has been included to show that point D is the minimum thickness (See
Figure 2).

References

1. S.W. Tsai, H.T. Hahn, Introduction to Composite Materials, Technomic Publishing Company, Westport, Connecticut, 1980.
2. D.M. Himmelblau, Applied Nonlinear Programming, McGraw-Hill, New York, 1972.

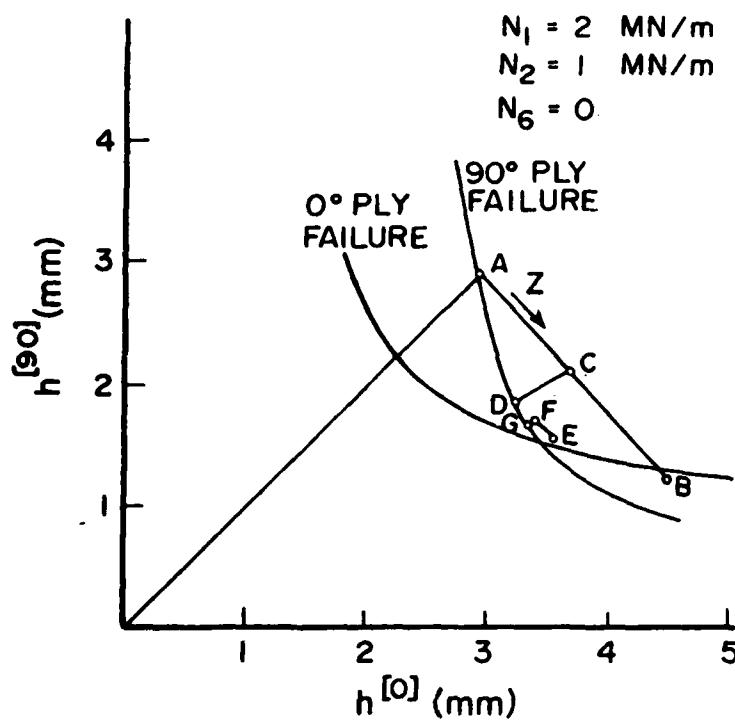


Figure 1. Constraint Surfaces and Optimization Trajectory for 0/90 under Biaxial Load.

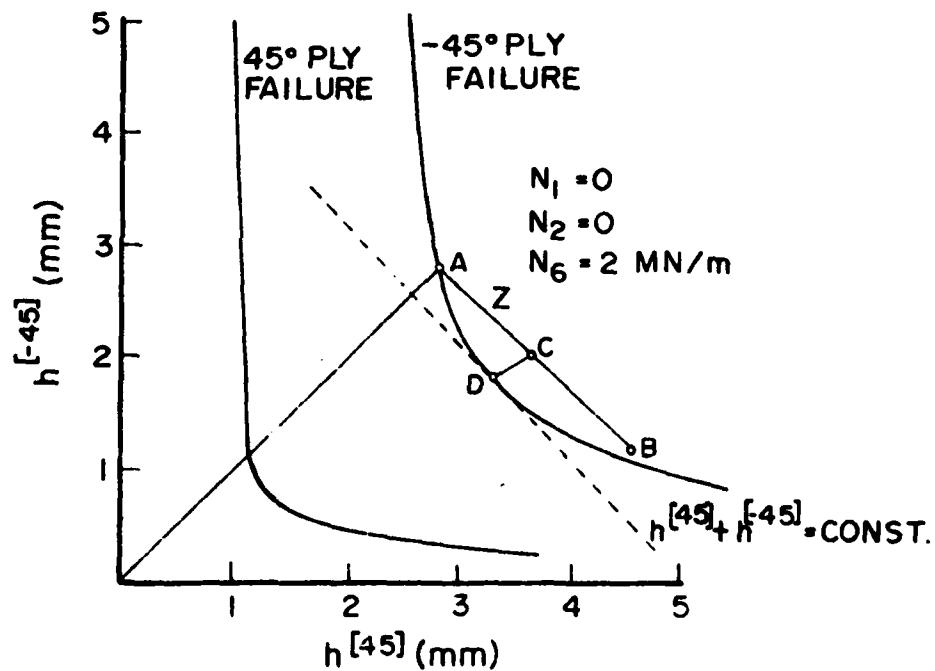
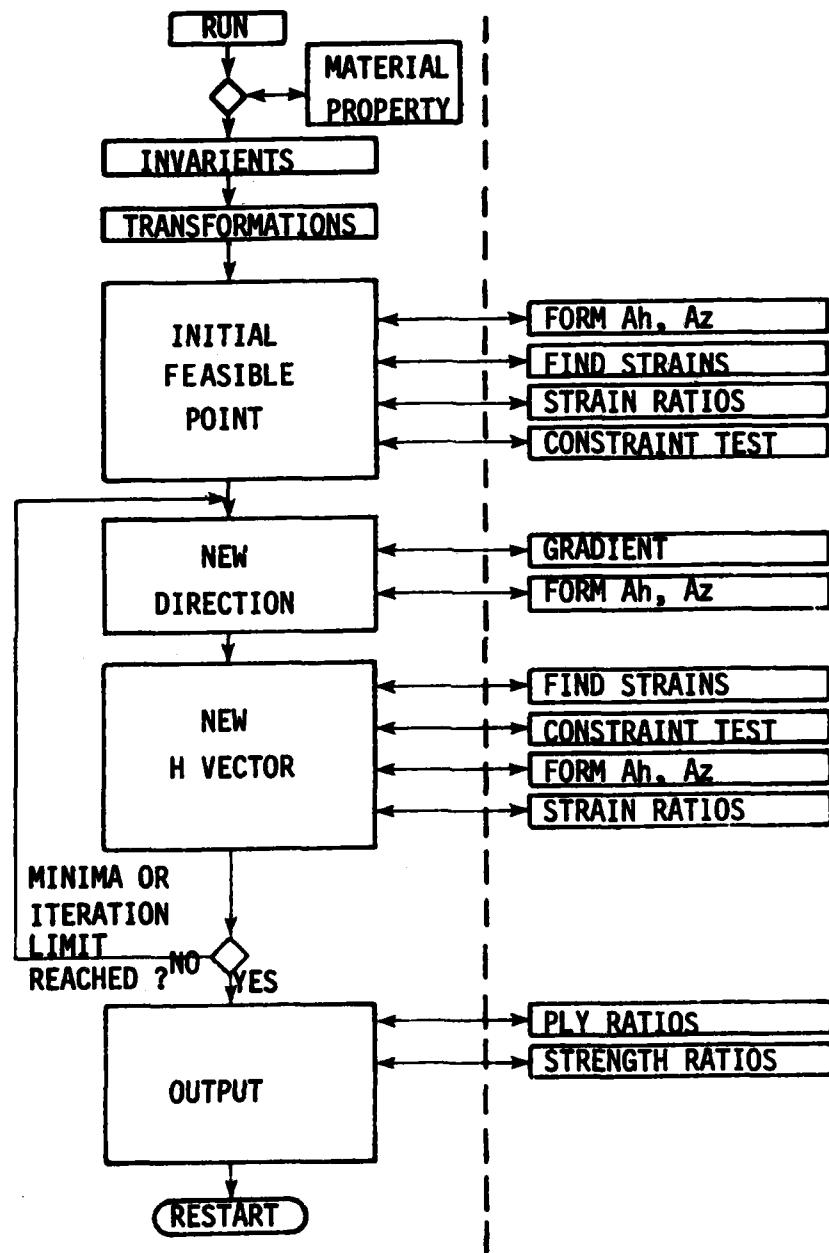


Figure 2. Constraint Surfaces and Optimization Trajectory for ± 45° Laminate Under Pure Shear.

APPENDIX A
FLOW DIAGRAM



APPENDIX B

KEY OPERATION PROCEDURE

DISPLAY	INPUT	PRINT OUT & REMARKS
MATERIAL NUMBER =	RUN [ENTER] 1 [ENTER]	T300/5208
NUMBER OF PLY ANGLES ? PLY ANGLE-1 ? PLY ANGLE-2 ?	2 [ENTER] 0 [ENTER] 90 [ENTER]	NO. OF PLY ANGLE= 2 ANGLE= 0.0 ANGLE= 90.0
NUMBER OF INDEPENDENT LOADINGS LOADING-1 N ₁ ? N ₂ ? N ₆ ? LOADING-2 N ₁ ? N ₂ ? N ₆ ?	2 [ENTER] 4 [ENTER] 1 [ENTER] 0 [ENTER] 1.25 [ENTER] 3.25 [ENTER] 1.299 [ENTER]	NO. OF LOADINGS= 2 LOADING UNIT is in MN/m LOADING-1 N ₁ = 4.000 N ₂ = 1.000 N ₆ = 0.000 LOADING-2 N ₁ = 1.250 N ₂ = 3.250 N ₆ = 1.299
		AFTER 4 ITERATIONS TOTAL THICKNESS = 2.282E 00 cm 132.57 PLIES

DISPLAY	INPUT	PRINT OUT & REMARKS																
		<p>ANGLE= 0.0 RATIO= 0.304 # PLIES= 55.63</p> <p>ANGLE= 90.0 RATIO= 0.695 # PLIES= 126.94</p> <p>STRENGTH RATIOS</p> <p>1=ULTIMATE STRAIN AND >1=SAFE</p> <table> <thead> <tr> <th colspan="2">LOADING-1</th> </tr> <tr> <th>PLY</th> <th>RATIO</th> </tr> </thead> <tbody> <tr> <td>0.0</td> <td>2.301</td> </tr> <tr> <td>90.0</td> <td>1.371</td> </tr> </tbody> </table> <table> <thead> <tr> <th colspan="2">LOADING-2</th> </tr> <tr> <th>PLY</th> <th>RATIO</th> </tr> </thead> <tbody> <tr> <td>0.0</td> <td>1.000</td> </tr> <tr> <td>90.0</td> <td>1.023</td> </tr> </tbody> </table>	LOADING-1		PLY	RATIO	0.0	2.301	90.0	1.371	LOADING-2		PLY	RATIO	0.0	1.000	90.0	1.023
LOADING-1																		
PLY	RATIO																	
0.0	2.301																	
90.0	1.371																	
LOADING-2																		
PLY	RATIO																	
0.0	1.000																	
90.0	1.023																	
MATERIAL NUMBER	[ON] [ENTER]	--BREAK--																

APPENDIX C
MEMORY CONTENTS

MEMORY	DESCRIPTION	MEMORY	DESCRIPTION
A(3,3)	Value of Thickness	Z(6)	Direction Vector
B(6,9)	G_{ij} (Strength Parameters in Strain Space)	A\$(6)	Subscript Indicators
C(6,9)	Q_{ij} (Modulus Components)	U1--U5	Modulus invariants
D(3,3)	$\Sigma Q_{ij}^k Z_k$	V1--V7	Strength invariants (Strain Space)
E(4,3)	Strains	C2	$\cos 2\theta$
G(3,3)	Strength Parameter Matrix	C4	$\cos 4\theta$
N(4,3)	Loads	S2	$\sin 2\theta$
P(3,3)	Inverse of A Matrix	S4	$\sin 4\theta$
Q(3,3)	Modulus Matrix	S	Final scalar distance to be moved
C\$(10,2)	List of active constraints	S1--S2	Points in feasible region
H(6)	Thickness for each ply	SR	Distance to origin
R(3)	Intermediate results	SM	Distance to first h=0 constraint
S(3)	Strength parameter components	NP	Number of ply orientations
T(6)	Angle of each ply	NL	Number of independent loadings

MEMORY CONTENTS (CONTINUED)

MEMORY	DESCRIPTION	MEMORY	DESCRIPTION
W(6)	Normalized gradient of a constraint	NC	Number of active constraints
X(6)	Normalized sum of gradients	IT	Iteration counter
Y(3)	Intermediate results	TP	Individual thickness
IM	Maximum number of iterations	GR,GS GP,GQ	Strength parameter in strain space
NN	$(1-v_x v_y)^{-1}$	GX,GY	
A, B, C, D, G, H, CN, NM, TS, SV	Intermediate calculations	F\$	Flag to halt program when "F"
		G\$	Flag "F" if a constraint is violated
I, J, K, L	Loop counters	M\$	Material Numbers
P, II	Ply orientation pointers	W\$	Material Names
N	Load pointers	X\$	Subscript indicators
Z	\sqrt{NP}		
O, Q, R, T	Engineering constants		
U, V, W, X, Y	Strengths		
Q1-Q4	Modulus		

APPENDIX D

(D) SAMPLE PROBLEMS

T300/5208

NO. OF PLY ANGLE = 2

ANGLE = -10.0

ANGLE = 70.0

NO. OF LOADINGS = 2

LOADING UNIT is
in MN/m

LOADING-1

N1 = 4.000

N2 = 1.000

N6 = 0.000

LOADING-2

N1 = 1.250

N2 = 3.250

N6 = 1.299

AFTER 5 ITERATIONS

TOTAL THICKNESS =

1.133E 00 cm

90.68 PLIES

ANGLE = -10.0

RATIO = 0.500

PLIES = 45.34

ANGLE = 70.0

RATIO = 0.500

PLIES = 45.34

STRENGTH RATIOS

λ = ULTIMATE STRAIN
AND λ_i = SAFE

LOADING-1

PLY RATIO

-12.0 1.388

72.0 1.000

LOADING-2

PLY RATIO

-12.0 1.068

72.0 1.000

T300/5208

NO. OF PLY ANGLE = 4

ANGLE = 0.0

ANGLE = 45.0

ANGLE = -45.0

ANGLE = 90.0

NO. OF LOADINGS = 4

LOADING UNIT is
in MN/m

LOADING-1

N1 = 1.000

N2 = 1.000

N6 = 1.000

LOADING-2

N1 = 2.000

N2 = 1.000

N6 = 0.000

LOADING-3

N1 = 2.000

N2 = -1.000

N6 = 0.000

LOADING-4

N1 = 0.000

N2 = 0.000

N6 = -1.500

AFTER 4 ITERATIONS

STRENGTH RATIOS

λ = ULTIMATE STRAIN
AND λ_i = SAFE

LOADING-1

PLY RATIO

0.0 1.320

45.0 2.271

-45.0 1.074

90.0 1.384

LOADING-2

PLY RATIO

0.0 1.839

45.0 1.476

-45.0 1.513

90.0 1.298

LOADING-3

PLY RATIO

0.0 2.396

45.0 1.260

-45.0 1.264

90.0 1.000

LOADING-4

PLY RATIO

0.0 1.269

45.0 1.010

-45.0 2.453

90.0 1.271

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T300/5208

NO. OF PLY ANGLE= 4
 ANGLE= 0.0
 ANGLE= 90.0
 ANGLE= 45.0
 ANGLE=-45.0

NO. OF LOADINGS= 2
 LOADING UNIT is
 in MN/m

LOADING-1

N1=	3.000
N2=	2.000
N6=	0.500

LOADING-2

N1=	1.000
N2=	4.000
N6=	0.000

AFTER 3 ITERATIONS

TOTAL THICKNESS =
 1.154E 00 cm
 92.32 PLIES

ANGLE= 0.0
 RATIO= 0.203
 # PLIES= 18.75

ANGLE= 90.0
 RATIO= 0.335
 # PLIES= 30.97

ANGLE= 45.0
 RATIO= 0.230
 # PLIES= 21.30

ANGLE=-45.0
 RATIO= 0.230
 # PLIES= 21.30

STRENGTH RATIOS

1=ULTIMATE STRAIN
 AND >1=SAFE

LOADING-1

PLY	RATIO
0.0	1.426
90.0	1.004
45.0	1.324
-45.0	1.043

LOADING-2

PLY	RATIO
0.0	1.000
90.0	1.769
45.0	1.220
-45.0	1.220

BORON/5505

NO. OF PLY ANGLE= 4
 ANGLE= 0.0
 ANGLE= 90.0
 ANGLE= 45.0
 ANGLE=-45.0

NO. OF LOADINGS= 2
 LOADING UNIT is
 in MN/m

LOADING-1

N1=	3.000
N2=	2.000
N6=	0.500

LOADING-2

N1=	1.000
N2=	4.000
N6=	0.000

AFTER 5 ITERATIONS

TOTAL THICKNESS =
 1.194E 00 cm
 95.56 PLIES

ANGLE= 0.0
 RATIO= 0.203
 # PLIES= 19.41

ANGLE= 90.0
 RATIO= 0.337
 # PLIES= 32.21

ANGLE= 45.0
 RATIO= 0.229
 # PLIES= 21.97

ANGLE=-45.0
 RATIO= 0.229
 # PLIES= 21.97

STRENGTH RATIOS

1=ULTIMATE STRAIN
 AND >1=SAFE

LOADING-1

PLY	RATIO
0.0	1.379
90.0	1.002
45.0	1.321
-45.0	1.046

LOADING-2

PLY	RATIO
0.0	1.000
90.0	1.654
45.0	1.300
-45.0	1.300

AS/3501

NO. OF PLY ANGLE= 4
 ANGLE= 0.0
 ANGLE= 90.0
 ANGLE= 45.0
 ANGLE=-45.0

NO. OF LOADINGS= 2
 LOADING UNIT is
 in MN/m

LOADING-1

N1=	3.000
N2=	2.000
N6=	0.500

LOADING-2

N1=	1.000
N2=	4.000
N6=	0.000

AFTER 7 ITERATIONS

TOTAL THICKNESS =
 1.000E 00 cm
 80.04 PLIES

ANGLE= 0.0
 RATIO= 0.203
 # PLIES= 16.26

ANGLE= 90.0
 RATIO= 0.333
 # PLIES= 26.67

ANGLE= 45.0
 RATIO= 0.231
 # PLIES= 18.56

ANGLE=-45.0
 RATIO= 0.231
 # PLIES= 18.56

STRENGTH RATIOS

1=ULTIMATE STRAIN
 AND >1=SAFE

LOADING-1

PLY	RATIO
0.0	1.362
90.0	1.019
45.0	1.287
-45.0	1.054

LOADING-2

PLY	RATIO
0.0	1.000
90.0	1.591
45.0	1.195
-45.0	1.195

APPENDIX E
PROGRAM LISTING

```

10: "OPTIM":CLEAR
12: DIM H(6), R(3),
      S(3), T(6), W(6)
      , X(6), Y(3), Z(6)
      )
14: DIM A(3,3), B(6
      , 9), C(6,9), D(3
      , 3), E(4,3), G(3
      , 3), N(4,3), P(3
      , 3), Q(3,3)
16: DIM A$(6), C$(1
      , 0,2)
18: IT=1: M=10
20: DATA "1", "2", "
      "3", "4", "5", "6"
21: RESTORE 20:FOR
      I=1TO 6:READ A
      $(I):NEXT I
30: GOSUB 1200
40: GOSUB 1700:
      GOSUB 1100:
      GOSUB 1000
42: GOSUB 800
45: IF F$="F" GOTO
      1300
50: GOSUB 700
60: IT=[T+]
70: IF F$="F" OR IT
      >IMTHEN GOTO 1
      300
75: GOTO 42
200: G$="P": NC=0
210: FOR P=1TO NP
215: IF H(P)=0 GOTO
      280
220: I=P: GOSUB 650
225: FOR N=1TO NL
230: CN=-1
235: FOR K=1TO 3:
      FOR J=1TO 3
240: CN=CN+G(K, J)*E
      (N, J)*E(N, K).
      NEXT J
245: CN=CN+S(K)*E(N
      , K).NEXT K
250: IF CN>0LET G$=
      "F": GOTO 295
253: IF CN<-1 GOTO
      275
255: NC=NC+1
260: C$(NC, 1)=CHR$
      P: C$(NC, 2)=
      CHR$ N
275: NEXT N
280: NEXT P
295: RETURN
300: NM=0, II=P:
      GOSUB 650
305: FOR L=1TO NP
310: IF H(L)=0 GOTO
      370
315: II=L: GOSUB 600
320: FOR J=1TO 3: R(
      J)=0
325: FOR K=1TO 3
330: R(J)=R(J)-Q(J,
      K)*E(N,K)
335: NEXT K: NEXT J
340: FOR J=1TO 3: Y(
      J)=0
342: FOR K=1TO 3: Y(
      J)=Y(J)+P(J, K)
      *R(K)
345: NEXT K: NEXT J
350: W(L)=0
352: FOR J=1TO 3:
      FOR K=1TO 3
354: W(L)=W(L)+G(J,
      K)*(Y(J)*E(N, K
      )+E(N, J)*Y(K))
356: NEXT K
358: W(L)=W(L)+S(J)
      *Y(J).NEXT J
360: NM=NM+W(L)*W(L
      )
370: NEXT L
375: NM=S(NM)
380: FOR L=1TO NP
385: W(L)=W(L)/NM.
      NEXT L
390: RETURN
400: FOR I=1TO 3:
      FOR J=1TO 3
405: E(I, J)=A(I, J)+
      D(I, J)*S
410: NEXT J: NEXT I
415: T=E(1, 1), U=E(1
      , 2), V=E(1, 3), W
      =E(2, 2), X=E(2,
      3), Y=E(3, 3)
420: D=T*X*Y+2*U*X-
      U-W*X*U-T*X*X-
      Y*U*U
425: F=(W*Y-X*X)/D
      Q=(T*Y-U*U)/D
      G=(U*X-U*Y)/D
430: R=(T*W-U*U)/D:
      H=(U*X-W*X)/D.
      O=(U*U-T*X)/D
435: P(1, 1)=F, P(1, 2
      )=G, P(1, 3)=H, P
      (2, 1)=G, P(2, 2)
      =O
440: P(2, 3)=Q, P(3, 1
      )=H, P(3, 2)=Q, P
      (3, 3)=R
450: FOR I=1TO NL:
      FOR J=1TO 3
455: E(I, J)=0
460: FOR K=1TO 3
470: E(I, J)=E(I, J)+
      P(J, K)*N(I, K)
480: NEXT K: NEXT J
490: NEXT I: RETURN
500: FOR I=1TO 3:
      FOR J=1TO 3
510: A(I, J)=0. D(I, J
      )=0
520: NEXT J: NEXT I
530: FOR I=1TO NP: I
      =I
540: GOSUB 600
550: FOR J=1TO 3:
      FOR K=1TO 3
560: A(J, K)=A(J, K)+
      Q(J, K)*H(I). D(
      J, K)=D(J, K)+Q(
      J, K)*Z(I)
570: NEXT K: NEXT J:
      NEXT I
580: RETURN
600: FOR J=1TO 3:
      FOR K=1TO 3
610: Q(J, K)=C(I, J*
      K)
620: NEXT K: NEXT J
640: RETURN
650: FOR J=1TO 3
      FOR K=1TO 3
660: G(J, K)=B(I, J*
      K)
670: NEXT K: NEXT J
680: S(1)=B(I, 1). S(
      2)=B(I, 8). S(
      3)=B(I, 5)
690: RETURN
700: SM=1E10
722: FOR I=1TO NP
734: IF Z(I)<>0LET
      S=-H(I)/Z(I)

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736: IF S>0 AND S<SM      810: P=ASC C$(I, 1):      1020: GOSUB 500
      THEN LET SM=S          N=ASC C$(I, 2):      1030: S=0, SR=1
737: NEXT I                  GOSUB 300          GOSUB 400
738: F$="P"                  812: FOR J=1 TO NP: X      1040: S=0, GOSUB 90
      814: NEXT J: NEXT I      (J)=X(J)-W(J)      0
740: IF SM>10 LET F$      816: FOR I=1 TO NP      1050: FOR I=1 TO NP
      ="F": RETURN          820: NM=0: FOR J=1 TO      H(I)=H(I)*S
      824: S1=0: S2=SM: S=S      NP          NEXT I
      M                      825: NM=NM+X(J)*X(J)      1060: S=0, GOSUB 50
      827: NEXT J              830: NM=J(NM): TS=0      0
      830: FOR I=1 TO NP: X      835: FOR I=1 TO NP
      (I)=X(I)/NM          840: TS=TS+X(I)*Z*      1070: GOSUB 400:
      845: Z(I)=X(I)-TS*Z      SGN H(I): NEXT      GOSUB 200:
      *SGN H(I)          850: FOR I=1 TO NP: X      RETURN
      855: TS=TS+X(I)*Z*      855: FOR I=1 TO NP
      SGN H(I): NEXT I      860: NM=0: FOR I=1 TO      1100: FOR I=1 TO NP
      865: Z(I)=X(I)-TS*Z      NP          1110: C2=COS (2*T(
      *SGN H(I)          870: NM=NM+Z(I)*Z(I)      I)): C4=COS (
      875: FOR I=1 TO NP: X      875: TS=TS+X(I)*Z*      4*T(I))
      (I)=H(I)+Z(I)*      880: NM=J(NM): TS=0      1120: S2=SIN (2*T(
      S          885: FOR I=1 TO NP: X      I)): S4=SIN (
      885: FOR I=1 TO NP: X      (I): TS=0      4*T(I))
      (I)=Z(I)/NM          890: FOR I=1 TO NP: X      1130: B(I, 1)=U1+C2
      895: FOR I=1 TO NP: X      (I)=Z(I)/NM:      *U2+C4*U3, B(
      (I)=H(I)+Z(I)*      900: FOR P=1 TO NP      I, 4)=U1-C2*U
      S          905: IF H(P)=0 GOTO      2+C4*U3
      910: I=1: GOSUB 650      910: FOR P=1 TO NP      1140: B(I, 2)=U4-C4
      915: FOR N=1 TO NL: B      915: FOR P=1 TO NP      *U3, B(I, 9)=U
      =0: C=0          920: FOR I=1 TO 3:      5-C4*U3
      920: FOR J=1 TO 3:      925: C=C-SR*S*G(I,
      925: C=C-SR*S*G(I,      J)*E(N, I)*E(N,
      J)*E(N, J)          930: NEXT J      1150: B(I, 3)=S2/2*
      930: NEXT J          940: B=B-SR*S*(I)*E(C      U2+S4*U3, B(I
      940: B=B-SR*S*(I)*E(C      N, I): NEXT I      , 6)=S2/2*U2-
      950: SU=(-B+J(B*B-4      950: SU=(-B+J(B*B-4      S4*U3
      *C*(I-1E-6))/      *C*(I-1E-6))/      1160: B(I, 7)=U6+C2
      '2*(I-1E-6))      '2*(I-1E-6))      *U7: B(I, 8)=U
      960: IF SU>S LET S=S      960: IF SU>S LET S=S      6-C2*U7: B(I,
      U          970: NEXT N      970: NEXT N      5)=S2*U7
      980: NEXT P: RETURN      980: NEXT P: RETURN
      980: Z=1/J(NP)          980: Z=1/J(NP)
      1010: FOR I=1 TO NP      1010: FOR I=1 TO NP
      Z(I)=Z(H(I))          Z(I)=Z(H(I))
      Z: NEXT I              Z: NEXT I

```

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1240:PAUSE "PLY A
NGLE-"+STR$(I):INPUT T(I)
1241:GOSUB 1810
1242:LPRINT " ANGLE=";T(I)
1245:NEXT I:LF(I)
1248:GOSUB 1830
1250:INPUT "NO. OF INDEP. LOADINGS=";NL
1252:LPRINT "NO. OF LOADINGS=";NL
1253:LPRINT " LADING UNIT is in M N/m ".LF(I)
1255:FOR I=1TO NL
:LPRINT " LADING-"+A$(I)
1256:FOR J=1TO 3
1260:L=J:IF J=3
LET L=6
1262:X$=" N"+A$(L)+"="
1265:GOSUB 1800
1267:LPRINT X$.
INPUT N(I,J)
:LF(-1)
1268:LPRINT N(I,J)
1269:N(I,J)=N(I,J)*1E6
1270:NEXT J:LF(I)
:NEXT I:
RETURN
1300:TS=0
1310:FOR I=1TO NP
1320:TS=TS+H(I):
NEXT I
1322:LPRINT "AFTER "+STR$(IT)+"
ITERATIONS".LF(I)
1325:GOSUB 1840
1330:LPRINT "TOTAL THICKNESS =";TS*100:LF(-1)
1340:LPRINT "
cm"
1345:B=INT ((TS/T P+.005)*100)
/100
1347:GOSUB 1850
1350:LPRINT " ";B;" PLIES"
1355:GOSUB 1500
1360:GOSUB 1400:
GOTO 20
1400:LF(I)
1405:LPRINT " LENGTH RATIOS
":LF(I)
1410:LPRINT " I=ULTIMATE STRAIN AND >1
=SAFE".LF(I)
1420:FOR I=1TO NL
1430:LPRINT " LOADING-"+STR$(I)
1440:LPRINT " PLANE":LF(-1)
1445:LPRINT "
RAT
IO"
1446:GOSUB 1450
1448:NEXT I:
RETURN
1450:FOR P=1TO NP
1452:IF H(P)=0
GOTO 1490
1455:II=P:GOSUB 6
50
1460:A=0:B=0
1465:FOR J=1TO 3:
FOR K=1TO 3
1470:A=A+G(J,K)*E(I,J)*E(I,K)
:NEXT K
1475:B=B+S(J)*E(I,J):NEXT J
1480:A=(-B+J*(B*B+
4*A))/2/A
1482:A=INT ((A+.5
/1E3)*1E3)/1
E3
1483:GOSUB 1810
1484:LPRINT " ";W(P):LF(-1)
1485:GOSUB 1800
1486:LPRINT A
1490:NEXT P
1495:LF(I):
RETURN
1500:FOR I=1TO NP
1505:LF(I)
1510:W(I)=INT ((T(I)+.05)*10)
/10
1520:A=INT ((H(I)
/TS+.5/1E4)*1E4)/1E4
1530:B=INT ((H(I)
/TP+.005)*10
/100
1535:GOSUB 1810
1540:LPRINT " ANGLE E=";W(I)
1545:GOSUB 1800
1550:LPRINT " RATIO D=";A
1555:GOSUB 1850
1560:LPRINT "# PLATES=";B
1570:NEXT I:
RETURN
1600:INPUT "MATERIAL NO.= ";M
$
1602:I=VAL M*$*10+
1600:GOSUB I
:RESTORE I:
READ W$,D,Q,
R,T,TP,U,U,W
,X,Y:LPRINT
W$:GOTO 1697
1610:DATA "T300/5
208", 181,.10
,3,.28,7,17,
125E-6, 1500,
1500, 40,.246
,68.:RETURN
1620:DATA "BORON/
5505", 204,.1
8.5,.23,5.59
,125E-6, 1260
,2500, 61,.20
2,.67.:
RETURN
1630:DATA "AS/350
1", 138,.8.96
,.30,7.1.125
E-6, 1447, 144
7,51.7,206.,
93.:RETURN
1640:DATA " "
RETURN
1650:DATA " "
RETURN
1660:DATA " "
RETURN
1670:DATA " "
RETURN
1680:DATA " "
RETURN
1690:DATA " "
RETURN
1692:RETURN

```

```

1700: Q=0*1E9, Q=Q*
    1E9, T=T*1E9,
    U=U*1E6, U=U*
    1E6, W=W*1E6,
    X=X*1E6, Y=Y*
    1E6
1705: NN=1/(1-R*R*
    0/0): Q1=NN*X
    : Q2=NN*Q: Q3=
    NN*R*Q: Q4=T
1710: U1=(3*Q1+3*Q
    2+2*Q3+4*Q4)
    /8: U2=(Q1-Q2
    )/2: U3=(Q1+Q
    2-2*Q3-4*Q4)
    /8
1720: U4=(Q1+Q2+6*
    Q3-4*Q4)/8: U
    5=(Q1+Q2-2*Q
    3+4*Q4)/8
1730: Q=1/(U*X): Q=
    1/(W*X): T=1/
    (Y*Y): G=1/U-
    1/U: H=1/W-1/
    X
1740: F=-J(U*Q)/2
1750: GP=0*Q1*Q1+2
    *F*Q1*Q3+Q*Q
    3*Q3, GQ=0*Q3
    *Q3+2*F*Q3*Q
    2+Q*Q2*Q2
1760: GR=0*Q1*Q3+F
    *(Q1*Q2+Q3*Q
    3)+Q*Q3*Q2: G
    S=T*Q4*Q4
1765: GX=G*Q1+H*Q3
    : GY=G*Q3+H*Q
    2
1770: U1=(3*GP+3*G
    Q+2*GR+4*GS)
    /8, U2=(GP-GQ
    )/2
1775: U3=(GP+GQ-2*
    GR-4*GS)/8: U
    4=(GP+GQ+6*G
    R-4*GS)/8
1780: U5=(GP+GQ-2*
    GR+4*GS)/8
1790: U6=(GX+GY)/2
    : U7=(GX-GY)/
    2, RETURN
1800: USING "###.#"
    "#": RETURN
1810: USING "###.#
    ".RETURN

```

END

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